

Control of chemical chaos through medium viscosity in a batch ferroin-catalysed Belousov-Zhabotinsky reaction

This is the peer reviewed version of the following article:
Original:
Budroni, M.A., Calabrese, I., Miele, Y., Rustici, M., Marchettini, N., Rossi, F. (2017). Control of chemical chaos through medium viscosity in a batch ferroin-catalysed Belousov-Zhabotinsky reaction. PHYSICAL CHEMISTRY CHEMICAL PHYSICS, 19(48), 32235-32241 [10.1039/c7cp06601e].
Availability:
This version is availablehttp://hdl.handle.net/11365/1033790 since 2018-02-26T12:07:03Z
Published:
DOI:10.1039/c7cp06601e
Terms of use:
Open Access
The terms and conditions for the reuse of this version of the manuscript are specified in the publishing policy. Works made available under a Creative Commons license can be used according to the terms and conditions of said license. For all terms of use and more information see the publisher's website.

(Article begins on next page)

View Article Online View Journal

PCCP

Accepted Manuscript

This article can be cited before page numbers have been issued, to do this please use: M. Budroni, I. Calabrese, Y. Miele, M. Rustici, N. Marchettini and F. Rossi, *Phys. Chem. Chem. Phys.*, 2017, DOI: 10.1039/C7CP06601E.



This is an Accepted Manuscript, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this Accepted Manuscript with the edited and formatted Advance Article as soon as it is available.

You can find more information about Accepted Manuscripts in the **author guidelines**.

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard <u>Terms & Conditions</u> and the ethical guidelines, outlined in our <u>author and reviewer resource centre</u>, still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this Accepted Manuscript or any consequences arising from the use of any information it contains.



rsc.li/pccp

Journal Name

DOI: 10.10 CONCEPTION

ARTICLE TYPE

Cite this: DOI: 10.1039/xxxxxxxxx

Received Date Accepted Date

DOI: 10.1039/xxxxxxxxx

www.rsc.org/journalname

Control of chemical chaos through medium viscosity in a batch ferroin-catalysed Belousov-Zhabotinsky reaction

Marcello Budroni,^{*a} Ilaria Calabrese,^b Ylenia Miele,^c Mauro Rustici,^a Nadia Marchettini^d and Federico Rossi^{*c}

In this paper we show that the active interplay of the nonlinear kinetics and transport phenomena in a chemical oscillator can be exploited to induce and control chaos. To this aim we use as a model system the ferroin-catalysed Belousov-Zhabotinsky (BZ) oscillating reaction, which is known to evolve to a characteristic chaotic transient dynamics when carried out in batch and unstirred conditions. In particular, chemical chaos was found to appear and disappear by following a Ruelle-Takens-Newhouse (RTN) scenario. Here we use the medium viscosity as a bifurcation parameter to tune the reaction-diffusion-convection (RDC) interplay and force the reaction in a specific sequence of dynamical regimes: either (*i*) periodic \rightarrow *quasi*-periodic \rightarrow chaotic or (*ii*) periodic \rightarrow *quasi*-periodic or (*iii*) only periodic. The medium viscosity can be set by adding different amounts of a surfactant (sodium dodecyl sulphate), known to have a little impact on the reaction mechanism, above its critical micelles concentration. Experimental results are supported by means of numerical simulations of a RDC model, which combines self-sustained oscillations to related chemically-induced buoyancy convection.

1 Introduction

Deterministic chaos is one of the most striking manifestation of the intrinsic complex mechanisms ruling the evolution of nonlinear dynamical systems. The appearance of chaotic regimes can be sometimes desirable, for example to enhance the mixing rate in a chemical reactor or as a means to encrypt binary messages and implement fundamental logic^{1,2}. However, most often, chaos is a phenomenon that has to be avoided or at least controlled. Many theoretical and experimental models have been developed to study and fine-tuning the innermost mechanisms responsible for the onset of chaotic dynamics in physical, mechanical, biological and chemical systems³. In particular, the Belousov-Zhabotisky (BZ) reaction⁴ is the most thoroughly studied chemical oscillator and still represents a paradigmatic model for understanding nonlinear dynamics in chemistry⁵. The BZ reaction is probably the simplest closed macroscopic system that can be maintained farfrom-equilibrium by an internal source of free energy⁶. During the catalytic oxidation of an organic substrate (generally malonic acid) by an oxy-halogen species (for example BrO_3^-) in acidic environment, oscillations in the intermediates and redox catalyst concentrations take place thanks to a complex nonlinear multistep reaction mechanism⁷.

When performed in open reactors (CSTR), the temporal behaviour of the BZ reaction is mainly dictated by the flow rate of the reactants, and can switch from periodic at low rates to complex oscillatory patterns (quasi-periodic and eventually chaotic) for higher rates $^{8-12}$.

In our previous studies^{13,14}, we demonstrated that temporal and spatio-temporal chaos may also arise when the BZ reaction is carried out in batch unstirred reactors. Chaos can be detected both via potentiometric and spectrophotometric techniques and typically appears as a transient dynamical regime, between two periodic areas, by following a direct and inverse Ruelle-Takens-Newhouse (RTN) scenario¹⁵, both in cerium- and ferroincatalysed BZ systems. The cerium catalysed reaction has been thoroughly characterised in several experimental conditions^{16–21} and the crucial role of the transport phenomena in the transition from periodic to aperiodic chemical oscillations has been assessed by means of theoretical models and numerical simulations^{22,23}. Chaotic oscillations are the result of the active interplay of the oscillations of the BZ intermediates with the related chemically-

^a Dipartimento di Chimica e Farmacia, Università di Sassari, Italy. E-mail: mabudroni@uniss.it

^b Istituto Zooprofilattico Sperimentale della Sicilia, Area Chimica e Tecnologie Alimentari, Palermo, Italy.

^c Department of Chemistry and Biology "A. Zambelli", University of Salerno, Italy; Email: frossi@unisa.it

^d Department of Earth, Environmental and Physical Sciences - DEEP Sciences, University of Siena, Italy.

driven convection.

In details, reaction-diffusion processes, that normally set-in in unstirred media, generate chemical patterns such as fronts and waves that feature local concentration heterogeneities spatially distributed through the reactive solution. If buoyancy- or/and surface-driven forces are at play, density and surface tension gradients associated to these chemical structures can trigger hydrodynamic flows that, in turn, couple with the spatio-temporal evolution of the reaction-diffusion structures. In general this active reaction-diffusion-convection (RDC) coupling, also called chemohydrodynamic coupling²⁴, can rule the overall dynamics of such systems and sustain complex spatio-temporal patterns^{25–35}. RDC dynamics can be governed and strongly depend on the experimental conditions of the system such as temperature, reactor size and reactants concentration, and on the changes that the chemical reaction is able to induce in the medium properties such as viscosity, density and surface tension. All these dependencies can be suitably included and described by pertinent dimensionless numbers (typically Grashof, Rayleigh and Marangoni numbers)²⁴.

Recently an externally forced RDC mechanism was also used to promote chaotic oscillations in a chemical system where a solution of a photochromic spiro-oxazine irradiated with UV light only at the bottom of the reactor develops convective motions combined with changes (switch between cis- and trans-) in the configuration of the spiro-oxazine. The resulting chaotic signals, recorded spectrophotometrically, were used to implement all the fundamental Boolean two-inputs-one-output logic gates^{2,36}.

In this paper we show how the cooperative interplay of an oscillatory kinetics and buoyancy-driven hydrodynamic instabilities can be exploited as a general pathway to initiate, *in-situ*, and control self-sustained chemical chaos. To this aim we use as a model system the ferroin catalysed BZ reaction and tune the solution viscosity, thus critically affecting the resistance of the reactive medium to hydrodynamic instabilities.

Experimentally, we introduce sodium dodecyl sulphate (SDS) anionic surfactant in the BZ medium and vary its concentration above the critical micelle concentration (CMC) to increase the solution viscosity. SDS was found to slightly alter the kinetics of the BZ reaction, without changing the oscillation mechanism and without introducing new dynamical features³⁷, conversely, for example, to the case of the zwitterionic surfactant *N*-tetradecyl-*N*,*N*-dimethylamine oxide that was found to cause an induction period prior the onset of regular oscillations^{38–40}. Therefore, the use of SDS impacts mainly the viscosity of the solution that, in turn, affects the onset of natural convection.

To support experimental scenarios we also develop a RDC model, where the kinetics of a chemical oscillator is coupled to fickian diffusion and convective terms, and we present related numerical simulations where the viscosity of the system is varied through the pertinent parameters.

2 Experimental

Malonic acid $(CH_2(COOH)_2, MA)$, sodium bromate $(NaBrO_3)$, sulfuric acid (H_2SO_4) , ferroin $(Fe(phen)_3^{2+}, Fe)$ and SDS were purchased from Sigma Aldrich. All reagents were of analytical quality and were used without further purification. Deionised

water from reverse osmosis (Elga, model Option 3) was used to prepare all the solutions. Reagents aqueous stock solutions were prepared, by weight, at the following concentrations: [MA] = 3.5 M, $[NaBrO_3] = 1.2$ M, $[H_2SO_4] = 5.0$ M, [Fe] = 25 mM, [SDS] = 0.7 M.

The kinetics of the BZ reaction has been studied at 25.0 °C, by keeping constant the concentration of all BZ reagents ([MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] = 0.35 M, [Fe] = 0.93 mM) in solutions with increasing concentration of surfactant, 0 < [SDS] < 100 mM).

The reaction dynamics was monitored by recording the absorption of ferriin, the oxidized form of ferroin, at $\lambda_{max} = 630$ nm ($\varepsilon = 620 \text{ M}^{-1} \text{ cm}^{-1}$) in a UV-vis spectrophotometer (Beckman DU-640 single ray) equipped with a water circulation cryo-thermostat (Haake D8). The solution for the kinetic runs were prepared in a 5 mL vial by adding the appropriate volumes of stock solutions, considering a final volume of 3.0 mL. The obtained solutions were stirred for twenty minutes with a magnetic stirrer, then, were transferred into quartz cuvettes and placed in the spectrophotometer for data acquisition. Each kinetic measurement has been repeated at least three times in order to check the reproducibility of the experimental results. The time series obtained in this way were subjected to statistical-mathematical analysis.

Surface tension measurements were performed in the presence of BZ reagents, excluding the catalyst, at concentrations used for kinetic experiments, in order to determine the Critical Micelle Concentration (CMC) of SDS in the experimental conditions. The measurements were made at a temperature of 25.0 °C by means of an Automatic-KSV Sigma tensiometer, using the Wilhelmy plate method.

The viscosity (η) measurements were performed, at temperature of 25.0 °C, by means of an Ostwald viscometer on BZ-free catalyst solutions, at different concentration of SDS. The densities (ρ) of the solutions were previously measured, in the same experimental conditions, by using a flow densimeter (model 03D Sodev inc.). The relative viscosity has been calculated with respect to the BZ solution without surfactant as reference, through the formula $\eta_{rel} = \frac{\eta}{\eta_0} = \frac{t}{t_0} \frac{\rho}{\rho_0}$, where *t* and t_0 are the elution time of the solution containing the surfactant and the reference solution, respectively.

3 Results and discussion

Figure 1 a) reports a typical spectrophotometric time series of a ferroin-catalyzed BZ reaction in batch unstirred conditions. The transient dynamical regime in the interval 300–2800 s has been demonstrated to be a genuine manifestation of chaotic behaviour¹⁴, which appears and disappears between two periodic regions through a RTN-type scenario. To control the viscosity of the solution, thus influencing the hydrodynamic motions responsible for the onset of the chaotic regime, several experiments with increasing concentrations of surfactant were performed.

The critical micelle concentration of SDS in our experimental conditions was estimated as the intersection point of the two linear plots, above and below the CMC, of the surface tension versus log of surfactant concentration. CMC was estimated about 9.6×10^{-4} M at 25.0 °C in the presence of [MA] = 0.74 M, [NaBrO₃] = 0.28

2|

Published on 16 November 2017. Downloaded by Gazi Universitesi on 18/11/2017 12:08:24

Published on 16 November 2017. Downloaded by Gazi Universitesi on 18/11/2017 12:08:24



Fig. 1 a) Ferroin-catalyzed BZ reaction in a batch unstirred reactor without SDS; red trace represents the chaotic transient between the two periodic regions (black trace). [MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] = 0.35 M, [Fe] = 0.93 mM [SDS] = 0 M. b) Relative viscosity of SDS solutions in the presence of [MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] = 0.35 M; the inset shows the zoom of the region 0 < [SDS] < 1 × 10⁻² M. c) Ferroin-catalyzed BZ reaction in a batch unstirred reactor in the presence of [SDS] = 1 × 10⁻² M; red trace represents the chaotic transient between the two periodic regions (black trace). Reactants concentrations are the same as in a).

M and $[H_2SO_4] = 0.35$ M. The lower value with respect to that in water (~ 8×10^{-3} M) is in line with the effect caused by the presence of electrolytes⁴¹. The viscosity for the solutions with [SDS] > CMC was successively measured by means of the Ostwald method and the trend is reported in Figure 1 b). η_{rel} starts to increase almost linearly with [SDS] above the CMC and has a sharp increase for [SDS] > 6×10^{-3} M, then, after a second linear region for 0.1 < [SDS] < 0.3 M, a second sharp increase is recorded for [SDS] > 0.3 M. Those jumps in the viscosity of the solutions are probably due to a change in the shape of the micelles and in the aggregation state of the surfactant³⁷.

To maximise the effect of the surfactant on the viscosity of the solutions, we started to add SDS above the CMC. However we could not detect any difference in the reaction dynamics up to [SDS] = 1.15×10^{-2} M; below this threshold the transient chaotic regime is still present, though with a shorter lifetime. As an example Figure 1 c) reports a timeseries where [SDS] = 1×10^{-2} M, corresponding to $\eta_{rel} = 1.02$, and the chaotic transient spans the interval 700–2200 s.

Figure 2 shows the transition to a *quasi*-periodic regime when the concentration of the surfactant is increased to [SDS] = 1.15×10^{-2} M, corresponding to $\eta_{rel} = 1.03$. In the RTN scenario, the transition from a chaotic to a periodic regime takes place through the progressive disappearance of fundamental oscillation frequencies that brings the system from a strange attractor to a limit cycle in the phase space. Intermediate, or *quasi*periodic, regimes are characterised by at least 2 fundamental oscillation frequencies (2D torus in the phase space); in principle *n*D tori (with $n \ge 3$) can be observed in the phase space, but they are generally unstable and tend to collapse into chaos. In



Fig. 2 Ferroin-catalyzed BZ reaction in a batch unstirred reactor in the presence of $[SDS] = 1.15 \times 10^{-2}$ M. [MA] = 0.74 M, $[NaBrO_3] = 0.28$ M, $[H_2SO_4] = 0.35$ M, [Fe] = 0.93 mM. a) Chaotic dynamics as revealed by the broadband amplitude spectrum of the Fourier transform in b). c) *Quasi*-periodic dynamics with 3 fundamental frequencies which ratio is an irrational number, as revealed by the Fourier transform in d).

this respect, the dynamics reported in Figure 2 is a nice example of such behaviour and it is also a convincing demonstration of the dependence upon the initial conditions of nonlinear systems. In fact, Figures 2 a) and c) show a BZ reaction performed in the same experimental conditions (reactants concentrations, temperature, preparation time, etc.) evolving into two different dynamical regimes, as shown by the Fourier transforms reported in panels b) and d). Panel b) shows the broadband amplitude spectrum typical of chaos and relative to the framed region of the timeseries in panel a); panel d) shows the amplitude spectrum relative to the framed region in panel c), where 3 fundamental frequencies ($f_1 = 0.0215$ Hz, $f_2 = 0.0200$ Hz and $f_3 = 0.0188$ Hz), which ratio is an irrational number, and their linear combinations can be detected. In several experiments performed at $\eta_{rel} = 1.03$, the occurrence of the two behaviours was nearly 50%, confirming that the 3D torus is unstable and meaning that the system is close to the bifurcation point.

By increasing further the surfactant concentration, we could menage to complete the RTN scenario and bring the system to a periodic regime. Figure 3 shows the timeseries for [SDS] = 1.25×10^{-2} M ($\eta_{rel} = 1.04$), where in the place of the chaotic transient and of the 3D torus is now present a 2D torus, as shown by the Fourier transform in panel b); here 2 frequencies with an irrational ratio ($f_1 = 0.361$ Hz and $f_2 = 0.0283$ Hz) and their linear combinations can be assigned to all the peaks in the spectrum. Finally, for [SDS] = 2.5×10^{-2} M ($\eta_{rel} = 1.10$) the timeseries reported in panel c) shows a periodic behaviour with only one fundamental frequency ($f_1 = 0.0215$ Hz) as reported in panel d). Both the 2D torus and the limit cycle, are stable manifolds in the phase-space.



Fig. 3 Ferroin-catalyzed BZ reaction in a batch unstirred reactor in the presence of a) [SDS] = 1.25×10^{-2} M showing a *quasi*-periodic dynamics with 2 fundamental frequencies as revealed by the Fourier transform in b); and c) [SDS] = 2.5×10^{-2} M showing a periodic dynamics with 1 fundamental frequency as revealed by the Fourier transform in d). [MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] = 0.35 M, [Fe] = 0.93 mM.

4 Numerical Simulations

Published on 16 November 2017. Downloaded by Gazi Universitesi on 18/11/2017 12:08:24

In order to asses viscosity as a convenient way to control the chemo-hydrodynamic coupling in the BZ medium and, hence, the transition through possible dynamical regimes, we investigate the BZ oscillations in a closed and unstirred reactor *via* a theoretical approach.

We model the system as a two-dimensional vertical slab (i.e. a vertical cut of the real three-dimensional spectrophotometric cuvette) in the coordinate system (x, z), with the gravitational field $\mathbf{g} = (0, -g)$ oriented against the vertical axis *z*. As shown in previous work, this two-dimensional description is a reliable approximation to the three-dimensional problem ^{22,27,29,31}. A set of reaction-diffusion-convection (RDC) equations is derived by coupling the chemical kinetics to diffusion through Fick's terms and to natural convection by means of the Navier-Stokes equations.

The presence of the surfactant SDS does not affect the oscillatory kinetics of the reaction which can be thus described by the well-known two-variables Oregonator model^{5,42}. This model simplifies the highly complex kinetic scheme of the BZ, reducing the large number of species to two main chemical variables and preserving the essential features of the BZ dynamics. The related equations are derived in the *pool chemical approximation*, i.e. neglecting the consumption of the initial reactants as it occurs on a longer time scale than chemical oscillations, and quasi-stationary conditions are maintained for a long time even in batch reactors. The kinetic equations, written in the dimensionless form by using the Oregonator time scale, t_0^{23} , are

$$\frac{\mathrm{d}c_1}{\mathrm{d}t} = \frac{1}{\varepsilon} \left[c_1(1-c_1) + fc_2 \frac{q-c_1}{q+c_2} \right] = f_1(c_1,c_2,\bar{\kappa}), \quad (1)$$

$$\frac{\mathrm{d}c_2}{\mathrm{d}t} = c_1 - c_2 = f_2(c_1, c_2) , \qquad (2)$$

1-7

where c_1 and c_2 are the dimensionless concentrations of the autocatalytic intermediate species HBrO₂ and the oxidized catalyst, respectively, and $\bar{\kappa}$ is the set of kinetic parameters, $\bar{\kappa} = \{\varepsilon, q, f\}$. The initial distributions of the chemical species are set as

$$c_1(0) = 0.8 \text{ if } 0 < \theta < 0.5$$
 (3)

$$= c_{1(ss)}$$
 elsewhere (4)

$$c_2(0) = c_{2(ss)} + \frac{\theta}{8\pi f}$$
 (5)

(where $c_{2(ss)} = c_{1(ss)} = q(f+1)/(f-1)$ and θ is the polar coordinate angle) to mimic inhomogeneous concentration profiles that typically occur in unstirred systems. These specific functions were used by Jahnke et al.⁴³ to initiate spiral waves in an analogous reaction-diffusion system. q and ε are kinetic parameters accounting for the excitability of the system and f is a stoichiometric factor included in the resetting step of the oscillatory scheme. This parameter allows one to set the system in an oscillatory regime when it ranges $[0.5, 1+\sqrt{2}]$ and we use f = 1.6; q is fixed arbitrarily to 0.01 instead that 0.0002 found by Tyson⁴², since increasing it up to a value 0.01 it has little effect on rotating-wave solutions while speeding up numerical simulations⁴³; $\varepsilon = 0.01$.

Hydrodynamic equations are derived in the Boussinesq approximation, i.e. assuming that density changes only affect the gravitational term, and the temperature terms are also neglected since it has been demonstrated that diffusion of chemicals is two orders of magnitude smaller than thermal diffusivity, thus representing the stronger source for the onset of convection ^{44–46}. The dimensionless form of the RDC system, written in the *vorticity–stream function* ($\omega - \psi$) form, reads (see details in ³¹)

$$\frac{\partial c_i}{\partial t} + D_V \left(u \frac{\partial c_i}{\partial x} + v \frac{\partial c_i}{\partial z} \right) = D_i \nabla^2 c_i + f_i(c_j, \bar{\kappa}) \ i, j = 1, 2 \ , \ (6)$$

$$\frac{\partial \omega}{\partial t} + D_{\nu} \left(u \frac{\partial \omega}{\partial x} + v \frac{\partial \omega}{\partial z} \right) = D_{\nu} \left(\nabla^2 \omega - \sum_i Gr_i \frac{\partial c_i}{\partial x} \right), \quad (7)$$

$$\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial z^2} = -\omega , \qquad (8)$$

$$u = \frac{\partial \psi}{\partial z}, \qquad (9)$$

$$v = -\frac{\partial \psi}{\partial x} \,. \tag{10}$$

The vorticity ω is defined as the curl of the dimensionless velocity field $(u, v)^T$ scaled over the velocity scale $v_0 = v/x_0$, where v is the kinematic viscosity of the BZ medium and x_0 our length characteristic scale. $D_i = Dt_0/x_0^2 = 0.00350$ is the dimensionless diffusivity, D being the dimensional diffusivities of the two species in the BZ medium assumed be independent of the surfactant concentration.

The dimensionless parameters depending explicitly on viscosity are:

- $D_v = v t_0 / x_0^2$, the dimensionless viscosity;
- The solutal Grashof number of the *i*-th species, Gr_i , defined as

$$Gr_i = \frac{1}{\rho_0} \frac{\partial \rho}{\partial c_i} \frac{C_i^0 x_0^3 g}{v^2}.$$
 (11)

Here *g* is the gravitational acceleration, $\frac{1}{\rho_0} \frac{\partial \rho}{\partial c_i}$ expresses the density variation due to concentration changes in the *i*-th intermediate with respect to the reference state ρ_0 characterizing the BZ medium and C_i^0 is the concentration scale of the *i*-th species^{5,23}. *Gr_i* control the chemo-hydrodynamic coupling as they quantify the contribution of each chemical species to density-driven convective flows. Increasing the medium viscosity decreases *Gr_i* and, more concretely, the intensity of natural convection sustained by isothermal concentration gradients. Following relation (11), *Gr_i* is positive if the *i*-th species increases the local density of the medium and negative otherwise.

By writing the system viscosity as

$$\mathbf{v} = \mathbf{v}_0 \times \mathbf{v}_{rel} \,, \tag{12}$$

where v_0 represents the kinematic viscosity of the aqueous BZ mixture, we can conveniently use v_{rel} as a direct dimensionless parameter to control the system dynamics as in the experiments. This allows to vary at once both D_v and Gr_i .

The equations system (6–10) is solved by using the Alternating Direction Implicit Method (ADI)⁴⁷ over the dimensionless spatial domain of length $L_x = 50$ and height $L_z = 50$, discretized with a 100×100 points grid. Solutions were not substantially altered by increasing the spatial grid density.

We apply no-slip boundary conditions for the fluid velocity (i.e. $\psi = 0$)⁴⁸ and no-flux boundary conditions for the chemical concentration fields at the rigid walls of the slab. Due to the stiffness of the Oregonator model, simulations are run using a small integration time step $h_t = 1 \times 10^{-5}$, that ensures numerically stable and convergent solutions.

Experimental data (namely spectrophotometric time series) report as a function of time the solution absorbance (which is directly correlated to the catalyst concentration) averaged over the spatial domain scanned by the spectrophotometric beam. To compare numerical simulations with real experiments, we build the simulation time series by reporting at each time step the mean concentration of the oxidized catalyst, $\langle c_2(x,z,t) \rangle$, averaged over the solving grid. The dynamics reported hereunder correspond to the transient regimes of the experiments where natural convection is fully set-in, i.e. after stirring is stopped and, if possible, transitions to aperiodic behaviour should be visible. These regimes are framed in the experimental time series shown above. Differently from experiments, the signals obtained in the simulations are stationary because, as mentioned above, the reactants depletion is neglected.

As a starting point of our parametric study, we consider the same value setting for which in our previous studies we obtained a chaos in the same system^{22,23,27}: $Gr_1 = Gr_2 = 12.1$, $D_v = 58.5$. The route from chemical chaos to regular periodic oscillations is



Fig. 4 Chaotic oscillations (a) and related amplitude Fourier spectrum (b) obtained for the RDC equations (6–10) with $v_{rel} = 1.00$.



Fig. 5 Time series (a) and related amplitude Fourier spectrum (b) of the quasi-periodic regime obtained for the RDC equations (6–10) with $v_{rel} = 1.10$. $a = 9f_2 - 11f_2$, $b = 3f_2 - 2f_1$, $c = f_1 + f_2$, $d = 4f_2 + 2f_1$, $e = 3f_1 + f_2$.

then followed by increasing the relative viscosity of the medium, and, accordingly, reducing the starting value of Gr_i by a factor $1/v_{rel}^2$, and increasing D_v by v_{rel} . In agreement with the experimental results, the system undergoes different dynamical regimes corresponding to a RTN scenario:

Chaotic regime. In Figure 4a we show the typical aperiodic behaviour corresponding to $v_{rel} = 1.00$. Similar dynamics are found in the range $v_{rel} \in [1.00, 1.04]$. Within this parametric window the time series present high sensitivity to initial conditions and the signals diverge one from each other if the initial concentrations of the chemical species are slightly varied. This is consistent with one of the most striking signatures of chaos. Also in Fig. 1.b, there is the amplitude FFT spectrum of the signal in panel a). This shows a typical broadband, almost continuous, spectrum describing the infinite number of frequencies composing these chaotic oscillations, with a main contribution for small frequencies around 0.4. To further test and characterize for chaos, we calculated in a previous work²² the largest Lyapunov exponent, λ , using the Rosestein algorithm from TISEAN package⁴⁹ and we obtained $\lambda = 0.018$.

Quasi-periodic regime. As the relative viscosity v_{rel} is increased to the value 1.05 a bifurcation to a quasi-periodic behavior is found (see Fig. 5). The toroidal nature of the flow in the related phase space is confirmed by the Fourier amplitude spectrum in Fig. 5.b. Here we show the two fundamental frequencies $f_1 \sim 0.4$, $f_2 \sim 0.59$ characterising this regime, along with their main linear combinations and their harmonics. Note that the dominant contribution f_1 also present in the broadband spectrum of the chaotic regime is preserved. The ratio f_1/f_2 is an irrational number as expected for quasi-periodic oscillations.

Physics Accepted Manuscri

Chemical

Chemistry

ysical (



Fig. 6 Time series (a) and related amplitude Fast Fourier spectrum (b) of the periodic regime obtained from the RDC equations (6–10) with $v_{rel} =$ 1.24.

Periodic regime. In Fig. 6 is shown a numerical experiment carried out for $v_{rel} = 1.24$. After a transient period (about 70 time units), the dynamics of the chemical species concentration switches to a regular periodic behaviour, here characterized by a limit cycle with one fundamental frequency $f_1 \sim 0.4$. Note that this frequency differs from that can be observed for the corresponding pure reaction-diffusion system ($f_1 \sim 0.75^{22}$), confirming the impact of the RDC interplay in the system dynamics. We observed that the frequency of the periodic oscillations increases to this limit as v_{rel} is further increased beyond the threshold 1.23.

5 Conclusion

To summarize, we investigated the RDC coupling in a chemical oscillator as a general method to induce and control *in-situ* chaos. The transition from periodic to chaotic behaviours is chemically triggered by self-sustained oscillations that, coupled to diffusion, sustain pattern formation and, concretely, concentration heterogeneities. The related density gradients, if the action of the gravitational field is at play, start buoyancy-driven hydrodynamic flows that can feedback and complicate the spatio-temporal evolution of the reaction and even lead to chaos.

The RDC interplay can be suitably ruled both via kinetic and hydrodynamic parameters. Here we showed experimentally that by increasing the viscosity of the ferroin-catalyzed BZ medium through the introduction of micellar SDS ionic surfactant, we can prevent the onset of the fingerprinting chaotic transient normally observed in the BZ carried out in aqueous solution.

Numerical simulations of the corresponding RDC model, where the Oregonator model is coupled to fickian diffusion and Navier-Stokes equations, agree with experimental results. They reveal a transition from a chaotic to a periodic regime by following a Ruelle-Takens-Newhouse scenario when the relative viscosity, affecting both the dimensionless viscosity and the Grashof numbers, is increased. Because of the batch conditions, an improved model should take into account the consumption of the reagents during the reaction evolution, however we already faced and modelled this feature in a previous work²³. Though we use some strong approximations in the system modelling, experimental features are not only qualitatively reproduced, but we can also find a semiquantitative matching with simulations. In particular we observe that a comparable increment in the relative viscosity induces analogous effects in the system dynamics both in numerical and real posed chemo-hydrodynamic mechanism in chemical oscillators as a source for self-sustained chaos and a means to control it. This approach can be further exploited for implementing fundamental Boolean two-inputs-one-output logic as in previous studies³⁶ and for Studying chaos synchronization in chemical systems.

Acknowledgments

This paper is dedicated to the memory of Prof. Maria Liria Turco Liveri, in whose Lab part of these results was obtained. F.R. was supported by the grants ORSA158121 and ORSA167988 funded by the University of Salerno (FARB ex 60%). MAB and MR acknowledge financial support from the Fondazione Banco di Sardegna and Regione Sardegna.

References

- 1 S. Boccaletti, C. Grebogi, Y.-C. Lai, H. Mancini and D. Maza, Physics Reports, 2000, 329, 103 – 197.
- 2 K. Hayashi, H. Gotoda and P. L. Gentili, Chaos: An Interdisciplinary Journal of Nonlinear Science, 2016, 26, 053102.
- 3 E. Ott, C. Grebogi and J. A. Yorke, Physical review letters, 1990, **64**, 1196.
- 4 B. P. Belousov, Sbornik Referatov po Radiatsonno Meditsine, Moscow, 1958, pp. 145-147.
- 5 S. K. Scott, Chemical Chaos, Oxford University Press, Oxford, UK, 1993.
- 6 A. M. Zhabotinsky and F. Rossi, International Journal of Ecodynamics, 2006, 1, 323-326.
- 7 A. F. Taylor, Progress in Reaction Kinetics and Mechanism, 2002, 27, 247-325.
- 8 J. Wang, P. G. Soerensen and F. Hynne, The Journal of Physical Chemistry, 1994, 98, 725-727.
- 9 J. C. Wang, P. G. Sorensen and F. Hynne, Zeitschrift Fur Physikalische Chemie-International Journal of Research, 1995, 192, 63-76.
- 10 B. R. Johnson, S. K. Scott and B. W. Thompson, Chaos: An Interdisciplinary Journal of Nonlinear Science, 1997, 7, 350-358.
- 11 P. E. Strizhak and A. L. Kawczynski, The Journal of Physical Chemistry, 1995, 99, 10830-10833.
- 12 J. Wang, J. Zhao, Y. Chen, Q. Gao and Y. Wang, Journal of *Physical Chemistry A*, 2005, **109**, 1374–1381.
- 13 M. Rustici, C. Caravati, E. Petretto, M. Branca and N. Marchettini, Journal of Physical Chemistry A, 1999, 103, 6564–6570.
- 14 F. Rossi, M. A. Budroni, N. Marchettini, L. Cutietta, M. Rustici and M. L. T. Liveri, Chemical Physics Letters, 2009, 480, 322-326.
- 15 S. Newhouse, D. Ruelle and F. Takens, Communications in Mathematical Physics, 1978, 64, 35-40.
- 16 N. Marchettini and M. Rustici, Chemical Physics Letters, 2000, 317, 647-651.
- 17 M. Rustici, R. Lombardo, M. Mangone, C. Sbriziolo, V. Zambrano and M. L. T. Liveri, Faraday Discussions, 2002, 120, 39-51.

- 18 M. Masia, N. Marchettini, V. Zambrano and M. Rustici, *Chemical Physics Letters*, 2001, **341**, 285–291.
- 19 M. L. T. Liveri, R. Lombardo, M. Masia, G. Calvaruso and M. Rustici, *Journal of Physical Chemistry A*, 2003, **107**, 4834– 4837.
- 20 F. Rossi, F. Pulselli, E. Tiezzi, S. Bastianoni and M. Rustici, *Chemical Physics*, 2005, **313**, 101–106.
- 21 L. Sciascia, F. Rossi, C. Sbriziolo, M. L. T. Liveri and R. Varsalona, *Physical Chemistry Chemical Physics*, 2010, **12**, 11674– 11682.
- 22 M. A. Budroni, M. Masia, M. Rustici, N. Marchettini, V. Volpert and P. C. Cresto, *The Journal of Chemical Physics*, 2008, **128**, 111102–4.
- 23 N. Marchettini, M. A. Budroni, F. Rossi, M. Masia, M. L. T. Liveri and M. Rustici, *Physical Chemistry Chemical Physics*, 2010, 12, 11062–11069.
- 24 A. D. Wit, K. Eckert and S. Kalliadasis, Chaos: An Interdisciplinary Journal of Nonlinear Science, 2012, 22, 037101.
- 25 K. Matthiessen and S. C. Müller, Phys. Rev. E, 1995, 52, 492– 495.
- 26 M. Diewald, K. Matthiessen, S. C. Müller and H. R. Brand, *Phys. Rev. Lett.*, 1996, **77**, 4466–4469.
- 27 M. A. Budroni, M. Masia, M. Rustici, N. Marchettini and V. Volpert, *The Journal of Chemical Physics*, 2009, 130, 024902–8.
- 28 L. Rongy and A. De Wit, Phys. Rev. E, 2008, 77, 046310.
- 29 L. Rongy, G. Schuszter, Z. Sinko, T. Toth, D. Horvath, A. Toth and A. D. Wit, *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 2009, **19**, 023110.
- 30 F. Rossi, M. A. Budroni, N. Marchettini and J. Carballido-Landeira, *Chaos: An Interdisciplinary Journal of Nonlinear Sci*ence, 2012, 22, 037109–037109–11.
- 31 M. A. Budroni, L. Rongy and A. De Wit, Phys. Chem. Chem. Phys., 2012, 14, 14619–14629.
- 32 I. Berenstein and C. Beta, *The Journal of Chemical Physics*, 2012, **136**, 034903.

- 33 D. M. Escala, M. A. Budroni, J. Carballido-Landeira, A. De Wit and A. P. Muñuzuri, *The Journal of Physical Chemistry Letters*, 2014, 5, 413–418.
- 34 R. Tiani, A. D. Wit and L. Rongy, Advances in Colloid and Interface Science, 2017.
- 35 M. A. Budroni and A. De Wit, *Chaos: An Interdisciplinary Jour*nal of Nonlinear Science, 2017, **27**, 104617.
- 36 P. L. Gentili, M. S. Giubila and B. M. Heron, *ChemPhysChem*, 2017, **18**, 1831–1841.
- 37 F. Rossi, R. Lombardo, L. Sciascia, C. Sbriziolo and M. L. T. Liveri, *Journal of Physical Chemistry B*, 2008, **112**, 7244– 7250.
- 38 F. Rossi, R. Varsalona and M. L. T. Liveri, Chemical Physics Letters, 2008, 463, 378–382.
- 39 F. Rossi, R. Varsalona, N. Marchettini and M. L. Turco Liveri, Soft Matter, 2011, 7, 9498.
- 40 M. A. Budroni and F. Rossi, *The Journal of Physical Chemistry C*, 2015, **119**, 9411–9417.
- 41 E. Dutkiewicz and A. Jakubowska, *Colloid and Polymer Science*, 2002, **280**, 1009–1014.
- 42 R. J. Field and M. Burger, Oscillations and Travelling Waves in Chemical Systems, Wiley, New York, USA, 1985.
- 43 W. Jahnke, W. E. Skaggs and A. T. Winfree, The Journal of Physical Chemistry, 1989, 93, 740–749.
- 44 Y. Wu, D. A. Vasquez, B. F. Edwards and J. W. Wilder, *Phys. Rev. E*, 1995, **51**, 1119–1127.
- 45 K. A. Cliffe, S. J. Tavener and H. Wilke, *Physics of Fluids*, 1998, 10, 730–741.
- 46 C. Almarcha, P. M. J. Trevelyan, P. Grosfils and A. De Wit, *Phys. Rev. E*, 2013, **88**, 033009.
- 47 D. W. Peaceman and H. H. Rachford, J. Soc. Ind. Appl. Math., 1955, 3, 28.
- 48 L. Lemaigre, M. A. Budroni, L. A. Riolfo, P. Grosfils and A. De Wit, *Physics of Fluids*, 2013, 25, 014103.
- 49 R. Hegger, H. Kantz and T. Schreiber, CHAOS, 1999, 9, 413.