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Control of chemical chaos through medium viscosity in a batch ferroin-catalysed Belousov-Zhabotinsky reaction

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In this paper we show that the active interplay of the nonlinear kinetics and transport phenomena in a chemical oscillator can be exploited to induce and control chaos. To this aim we use as a model system the ferroin-catalysed Belousov-Zhabotinsky (BZ) oscillating reaction, which is known to evolve to a characteristic chaotic transient dynamics when carried out in batch and unstirred conditions. In particular, chemical chaos was found to appear and disappear by following a Ruelle-Takens-Newhouse (RTN) scenario. Here we use the medium viscosity as a bifurcation parameter to tune the reaction-diffusion-convection (RDC) interplay and force the reaction in a specific sequence of dynamical regimes: either (*i*) periodic \rightarrow *quasi*-periodic \rightarrow chaotic or (*ii*) periodic \rightarrow *quasi*-periodic or (*iii*) only periodic. The medium viscosity can be set by adding different amounts of a surfactant (sodium dodecyl sulphate), known to have a little impact on the reaction mechanism, above its critical micelles concentration. Experimental results are supported by means of numerical simulations of a RDC model, which combines self-sustained oscillations to related chemically-induced buoyancy convection. JOUTINE IN ARTICLE TYPE

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1 Introduction

Deterministic chaos is one of the most striking manifestation of the intrinsic complex mechanisms ruling the evolution of nonlinear dynamical systems. The appearance of chaotic regimes can be sometimes desirable, for example to enhance the mixing rate in a chemical reactor or as a means to encrypt binary messages and implement fundamental logic $1,2$ $1,2$. However, most often, chaos is a phenomenon that has to be avoided or at least controlled. Many theoretical and experimental models have been developed to study and fine-tuning the innermost mechanisms responsible for the onset of chaotic dynamics in physical, mechanical, biological and chemical systems³. In particular, the Belousov-Zhabotisky (BZ) reaction^{[4](#page-7-3)} is the most thoroughly studied chemical oscillator and still represents a paradigmatic model for understanding nonlinear dynamics in chemistry⁵. The BZ reaction is probably the simplest closed macroscopic system that can be maintained farfrom-equilibrium by an internal source of free energy⁶. During the catalytic oxidation of an organic substrate (generally malonic acid) by an oxy-halogen species (for example BrO_3^-) in acidic environment, oscillations in the intermediates and redox catalyst concentrations take place thanks to a complex nonlinear multistep reaction mechanism⁷.

When performed in open reactors (CSTR), the temporal behaviour of the BZ reaction is mainly dictated by the flow rate of the reactants, and can switch from periodic at low rates to complex oscillatory patterns (quasi-periodic and eventually chaotic) for higher rates $8-12$ $8-12$.

In our previous studies $13,14$ $13,14$, we demonstrated that temporal and spatio-temporal chaos may also arise when the BZ reaction is carried out in batch unstirred reactors. Chaos can be detected both via potentiometric and spectrophotometric techniques and typically appears as a transient dynamical regime, between two periodic areas, by following a direct and inverse Ruelle-Takens-Newhouse (RTN) scenario 15 , both in cerium- and ferroincatalysed BZ systems. The cerium catalysed reaction has been thoroughly characterised in several experimental conditions^{16-[21](#page-8-0)} and the crucial role of the transport phenomena in the transition from periodic to aperiodic chemical oscillations has been assessed by means of theoretical models and numerical simulations [22,](#page-8-1)[23.](#page-8-2) Chaotic oscillations are the result of the active interplay of the oscillations of the BZ intermediates with the related chemically-

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In details, reaction-diffusion processes, that normally set-in in unstirred media, generate chemical patterns such as fronts and waves that feature local concentration heterogeneities spatially distributed through the reactive solution. If buoyancy- or/and surface-driven forces are at play, density and surface tension gradients associated to these chemical structures can trigger hydrodynamic flows that, in turn, couple with the spatio-temporal evolution of the reaction-diffusion structures. In general this active reaction-diffusion-convection (RDC) coupling, also called chemohydrodynamic coupling 24 , can rule the overall dynamics of such systems and sustain complex spatio-temporal patterns^{[25](#page-8-5)–35}. RDC dynamics can be governed and strongly depend on the experimental conditions of the system such as temperature, reactor size and reactants concentration, and on the changes that the chemical reaction is able to induce in the medium properties such as viscosity, density and surface tension. All these dependencies can be suitably included and described by pertinent dimensionless numbers (typically Grashof, Rayleigh and Marangoni numbers)²⁴. delocation-time interaction account the crossing tele-cosmic scale for the signific model (a) and 0, in α in the signific model interaction and interaction and interaction and interaction and interaction and interactio

Recently an externally forced RDC mechanism was also used to promote chaotic oscillations in a chemical system where a solution of a photochromic spiro-oxazine irradiated with UV light only at the bottom of the reactor develops convective motions combined with changes (switch between cis- and trans-) in the configuration of the spiro-oxazine. The resulting chaotic signals, recorded spectrophotometrically, were used to implement all the fundamental Boolean two-inputs-one-output logic gates^{[2](#page-7-1),36}.

In this paper we show how the cooperative interplay of an oscillatory kinetics and buoyancy-driven hydrodynamic instabilities can be exploited as a general pathway to initiate, *in-situ*, and control self-sustained chemical chaos. To this aim we use as a model system the ferroin catalysed BZ reaction and tune the solution viscosity, thus critically affecting the resistance of the reactive medium to hydrodynamic instabilities.

Experimentally, we introduce sodium dodecyl sulphate (SDS) anionic surfactant in the BZ medium and vary its concentration above the critical micelle concentration (CMC) to increase the solution viscosity. SDS was found to slightly alter the kinetics of the BZ reaction, without changing the oscillation mechanism and without introducing new dynamical features 37 , conversely, for example, to the case of the zwitterionic surfactant *N*-tetradecyl-*N,N*-dimethylamine oxide that was found to cause an induction period prior the onset of regular oscillations³⁸⁻⁴⁰. Therefore, the use of SDS impacts mainly the viscosity of the solution that, in turn, affects the onset of natural convection.

To support experimental scenarios we also develop a RDC model, where the kinetics of a chemical oscillator is coupled to fickian diffusion and convective terms, and we present related numerical simulations where the viscosity of the system is varied through the pertinent parameters.

2 Experimental

Malonic acid $(CH_2(COOH)_2, MA)$, sodium bromate (NaBrO₃), sulfuric acid (H₂SO₄), ferroin (Fe(phen) $_3^{2+}$, Fe) and SDS were purchased from Sigma Aldrich. All reagents were of analytical quality and were used without further purification. Deionised water from reverse osmosis (Elga, model Option 3) was used to prepare all the solutions. Reagents aqueous stock solutions were prepared, by weight, at the following concentrations: [MA] = 3.5 M, $[NaBrO₃] = 1.2 M$, $[H₂SO₄] = 5.0 M$, $[Fe] = 25 mM$, $[SDS]$ $= 0.7 M$.

The kinetics of the BZ reaction has been studied at 25.0 °C , by keeping constant the concentration of all BZ reagents ([MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] = 0.35 M, [Fe] = 0.93 mM) in solutions with increasing concentration of surfactant, $0 <$ [SDS] $<$ 100 mM).

The reaction dynamics was monitored by recording the absorption of ferriin, the oxidized form of ferroin, at $\lambda_{max} = 630$ nm (ε $= 620$ M⁻¹ cm⁻¹) in a UV-vis spectrophotometer (Beckman DU-640 single ray) equipped with a water circulation cryo-thermostat (Haake D8). The solution for the kinetic runs were prepared in a 5 mL vial by adding the appropriate volumes of stock solutions, considering a final volume of 3.0 mL. The obtained solutions were stirred for twenty minutes with a magnetic stirrer, then, were transferred into quartz cuvettes and placed in the spectrophotometer for data acquisition. Each kinetic measurement has been repeated at least three times in order to check the reproducibility of the experimental results. The time series obtained in this way were subjected to statistical-mathematical analysis.

Surface tension measurements were performed in the presence of BZ reagents, excluding the catalyst, at concentrations used for kinetic experiments, in order to determine the Critical Micelle Concentration (CMC) of SDS in the experimental conditions. The measurements were made at a temperature of 25.0 \degree C by means of an Automatic-KSV Sigma tensiometer, using the Wilhelmy plate method.

The viscosity (η) measurements were performed, at temperature of 25.0 \degree C, by means of an Ostwald viscometer on BZ-free catalyst solutions, at different concentration of SDS. The densities (ρ) of the solutions were previously measured, in the same experimental conditions, by using a flow densimeter (model 03D Sodev inc.). The relative viscosity has been calculated with respect to the BZ solution without surfactant as reference, through the formula $\eta_{rel} = \frac{\eta}{\eta_0} = \frac{t}{t_0} \frac{\rho}{\rho_0}$, where *t* and *t*₀ are the elution time of the solution containing the surfactant and the reference solution, respectively.

3 Results and discussion

Figure [1](#page-4-0) a) reports a typical spectrophotometric time series of a ferroin-catalyzed BZ reaction in batch unstirred conditions. The transient dynamical regime in the interval 300–2800 s has been demonstrated to be a genuine manifestation of chaotic behaviour [14,](#page-7-10) which appears and disappears between two periodic regions through a RTN-type scenario. To control the viscosity of the solution, thus influencing the hydrodynamic motions responsible for the onset of the chaotic regime, several experiments with increasing concentrations of surfactant were performed.

The critical micelle concentration of SDS in our experimental conditions was estimated as the intersection point of the two linear plots, above and below the CMC, of the surface tension versus log of surfactant concentration. CMC was estimated about 9.6×10^{-4} M at 25.0 °C in the presence of [MA] = 0.74 M, [NaBrO₃] = 0.28

Fig. 1 a) Ferroin-catalyzed BZ reaction in a batch unstirred reactor without SDS; red trace represents the chaotic transient between the two periodic regions (black trace). [MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] $= 0.35$ M, $[Fe] = 0.93$ mM $[SDS] = 0$ M. b) Relative viscosity of SDS solutions in the presence of [MA] = 0.74 M, [NaBrO₃] = 0.28 M, [H₂SO₄] = 0.35 M; the inset shows the zoom of the region $0 <$ [SDS] $< 1 \times 10^{-2}$ M. c) Ferroin-catalyzed BZ reaction in a batch unstirred reactor in the presence of $[SDS] = 1 \times 10^{-2}$ M; red trace represents the chaotic transient between the two periodic regions (black trace). Reactants concentrations are the same as in a).

M and $[H_2SO_4] = 0.35$ M. The lower value with respect to that in water ($\sim 8 \times 10^{-3}$ M) is in line with the effect caused by the presence of electrolytes⁴¹. The viscosity for the solutions with [SDS] *>* CMC was successively measured by means of the Ost-wald method and the trend is reported in Figure [1](#page-4-0) b). η_{rel} starts to increase almost linearly with [SDS] above the CMC and has a sharp increase for [SDS] $> 6 \times 10^{-3}$ M, then, after a second linear region for 0.1 *<* [SDS] *<* 0.3 M, a second sharp increase is recorded for [SDS] *>* 0*.*3 M. Those jumps in the viscosity of the solutions are probably due to a change in the shape of the micelles and in the aggregation state of the surfactant 37 .

To maximise the effect of the surfactant on the viscosity of the solutions, we started to add SDS above the CMC. However we could not detect any difference in the reaction dynamics up to [SDS] = 1.15×10^{-2} M; below this threshold the transient chaotic regime is still present, though with a shorter lifetime. As an example Figure [1](#page-4-0) c) reports a timeseries where [SDS] = 1×10^{-2} M, corresponding to η_{rel} = 1.02, and the chaotic transient spans the interval 700–2200 s.

Figure [2](#page-4-1) shows the transition to a *quasi*-periodic regime when the concentration of the surfactant is increased to [SDS] = 1.15×10^{-2} M, corresponding to $\eta_{rel} = 1.03$. In the RTN scenario, the transition from a chaotic to a periodic regime takes place through the progressive disappearance of fundamental oscillation frequencies that brings the system from a strange attractor to a limit cycle in the phase space. Intermediate, or *quasi*periodic, regimes are characterised by at least 2 fundamental oscillation frequencies (2D torus in the phase space); in principle *n*D tori (with $n \geq 3$) can be observed in the phase space, but they are generally unstable and tend to collapse into chaos. In

Fig. 2 Ferroin-catalyzed BZ reaction in a batch unstirred reactor in the presence of $[SDS] = 1.15 \times 10^{-2}$ M. $[MA] = 0.74$ M, $[NaBrO₃] = 0.28$ M, $[H₂SO₄] = 0.35 M$, [Fe] = 0.93 mM. a) Chaotic dynamics as revealed by the broadband amplitude spectrum of the Fourier transform in b). c) *Quasi*-periodic dynamics with 3 fundamental frequencies which ratio is an irrational number, as revealed by the Fourier transform in d).

this respect, the dynamics reported in Figure [2](#page-4-1) is a nice example of such behaviour and it is also a convincing demonstration of the dependence upon the initial conditions of nonlinear systems. In fact, Figures [2](#page-4-1) a) and c) show a BZ reaction performed in the same experimental conditions (reactants concentrations, temperature, preparation time, etc.) evolving into two different dynamical regimes, as shown by the Fourier transforms reported in panels b) and d). Panel b) shows the broadband amplitude spectrum typical of chaos and relative to the framed region of the timeseries in panel a); panel d) shows the amplitude spectrum relative to the framed region in panel c), where 3 fundamental frequencies ($f_1 = 0.0215$ Hz, $f_2 = 0.0200$ Hz and $f_3 = 0.0188$ Hz), which ratio is an irrational number, and their linear combinations can be detected. In several experiments performed at $\eta_{rel} = 1.03$, the occurrence of the two behaviours was nearly 50%, confirming that the 3D torus is unstable and meaning that the system is close to the bifurcation point. The contract of the contract

By increasing further the surfactant concentration, we could menage to complete the RTN scenario and bring the system to a periodic regime. Figure [3](#page-5-0) shows the timeseries for [SDS] $= 1.25 \times 10^{-2}$ M ($\eta_{rel} = 1.04$), where in the place of the chaotic transient and of the 3D torus is now present a 2D torus, as shown by the Fourier transform in panel b); here 2 frequencies with an irrational ratio ($f_1 = 0.361$ Hz and $f_2 = 0.0283$ Hz) and their linear combinations can be assigned to all the peaks in the spectrum. Finally, for [SDS] = 2.5×10^{-2} M (η_{rel} = 1.10) the timeseries reported in panel c) shows a periodic behaviour with only one fundamental frequency $(f_1 = 0.0215 \text{ Hz})$ as reported in panel d). Both the 2D torus and the limit cycle, are stable manifolds in the phase-space.

Fig. 3 Ferroin-catalyzed BZ reaction in a batch unstirred reactor in the presence of a) $[SDS] = 1.25 \times 10^{-2}$ M showing a *quasi*-periodic dynamics with 2 fundamental frequencies as revealed by the Fourier transform in b); and c) $[SDS] = 2.5 \times 10^{-2}$ M showing a periodic dynamics with 1 fundamental frequency as revealed by the Fourier transform in d). [MA] = 0.74 M, $[NaBrO₃]$ = 0.28 M, $[H₂SO₄]$ = 0.35 M, $[Fe]$ = 0.93 mM.

4 Numerical Simulations

In order to asses viscosity as a convenient way to control the chemo-hydrodynamic coupling in the BZ medium and, hence, the transition through possible dynamical regimes, we investigate the BZ oscillations in a closed and unstirred reactor *via* a theoretical approach.

We model the system as a two-dimensional vertical slab (i.e. a vertical cut of the real three-dimensional spectrophotometric cuvette) in the coordinate system (x, z) , with the gravitational field $g = (0, -g)$ oriented against the vertical axis *z*. As shown in previous work, this two-dimensional description is a reliable ap-proximation to the three-dimensional problem^{[22](#page-8-1)[,27](#page-8-12)[,29,](#page-8-13)31}. A set of reaction-diffusion-convection (RDC) equations is derived by coupling the chemical kinetics to diffusion through Fick's terms and to natural convection by means of the Navier-Stokes equations.

The presence of the surfactant SDS does not affect the oscillatory kinetics of the reaction which can be thus described by the well-known two-variables Oregonator model^{[5](#page-7-4),42}. This model simplifies the highly complex kinetic scheme of the BZ, reducing the large number of species to two main chemical variables and preserving the essential features of the BZ dynamics. The related equations are derived in the *pool chemical approximation*, i.e. neglecting the consumption of the initial reactants as it occurs on a longer time scale than chemical oscillations, and quasi-stationary conditions are maintained for a long time even in batch reactors. The kinetic equations, written in the dimensionless form by using the Oregonator time scale, t_0 ²³, are

$$
\frac{dc_1}{dt} = \frac{1}{\varepsilon} \left[c_1 (1 - c_1) + f c_2 \frac{q - c_1}{q + c_2} \right] = f_1(c_1, c_2, \bar{\kappa}), \quad (1)
$$

$$
\frac{dc_2}{dt} = c_1 - c_2 = f_2(c_1, c_2) ,
$$
\n(2)

where c_1 and c_2 are the dimensionless concentrations of the autocatalytic intermediate species $HBrO₂$ and the oxidized catalyst, respectively, and $\bar{\kappa}$ is the set of kinetic parameters, $\bar{\kappa} = {\epsilon, q, f}$. The initial distributions of the chemical species are set as

$$
c_1(0) = 0.8 \text{ if } 0 < \theta < 0.5 \tag{3}
$$

$$
= c_{1(ss)} \text{ elsewhere} \tag{4}
$$

$$
c_2(0) = c_{2(ss)} + \frac{\theta}{8\pi f}
$$
 (5)

(where $c_{2(ss)} = c_{1(ss)} = \frac{q(f+1)}{f-1}$ and θ is the polar coordinate angle) to mimic inhomogeneous concentration profiles that typically occur in unstirred systems. These specific functions were used by Jahnke et al.^{[43](#page-8-16)} to initiate spiral waves in an analogous reaction-diffusion system. q and ε are kinetic parameters accounting for the excitability of the system and *f* is a stoichiometric factor included in the resetting step of the oscillatory scheme. This parameter allows one to set the system in an oscillatory regime when it ranges [0.5, $1+\sqrt{2}$] and we use $f = 1.6$; *q* is fixed arbitrarily to 0.01 instead that 0.0002 found by Tyson⁴², since increasing it up to a value 0*.*01 it has little effect on rotating-wave solutions while speeding up numerical simulations⁴³; $\varepsilon = 0.01$.

Hydrodynamic equations are derived in the Boussinesq approximation, i.e. assuming that density changes only affect the gravitational term, and the temperature terms are also neglected since it has been demonstrated that diffusion of chemicals is two orders of magnitude smaller than thermal diffusivity, thus representing the stronger source for the onset of convection $44-46$ $44-46$. The dimensionless form of the RDC system, written in the *vorticity*–*stream function* ($\omega - \psi$) form, reads (see details in³¹)

$$
\frac{\partial c_i}{\partial t} + D_v \left(u \frac{\partial c_i}{\partial x} + v \frac{\partial c_i}{\partial z} \right) = D_i \nabla^2 c_i + f_i(c_j, \bar{\kappa}) \ i, j = 1, 2 \ , \ (6)
$$

$$
\frac{\partial \omega}{\partial t} + D_V \left(u \frac{\partial \omega}{\partial x} + v \frac{\partial \omega}{\partial z} \right) = D_V \left(\nabla^2 \omega - \sum_i G r_i \frac{\partial c_i}{\partial x} \right), \quad (7)
$$

$$
\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial z^2} = -\omega , \qquad (8)
$$

$$
u = \frac{\partial \psi}{\partial z}, \qquad (9)
$$

$$
v = -\frac{\partial \psi}{\partial x}.
$$
 (10)

The vorticity ω is defined as the curl of the dimensionless velocity field $(u, v)^T$ scaled over the velocity scale $v_0 = v/x_0$, where *v* is the kinematic viscosity of the BZ medium and x_0 our length characteristic scale. $D_i = Dt_0 / x_0^2 = 0.00350$ is the dimensionless diffusivity, *D* being the dimensional diffusivities of the two species in the BZ medium assumed be independent of the surfactant concentration.

The dimensionless parameters depending explicitly on viscosity are:

- $D_v = vt_0/x_0^2$, the dimensionless viscosity;
- *•* The solutal Grashof number of the *i*–th species, *Gri*, defined as

$$
Gr_i = \frac{1}{\rho_0} \frac{\partial \rho}{\partial c_i} \frac{C_i^0 x_0^3 g}{v^2}.
$$
 (11)

Here *g* is the gravitational acceleration, $\frac{1}{\rho_0} \frac{\partial \rho}{\partial c_i}$ expresses the density variation due to concentration changes in the *i*-th intermediate with respect to the reference state ρ_0 characterizing the BZ medium and C_i^0 is the concentration scale of the *i*-th species^{[5,](#page-7-4)23}. Gr_i control the chemo-hydrodynamic coupling as they quantify the contribution of each chemical species to density-driven convective flows. Increasing the medium viscosity decreases *Gri* and, more concretely, the intensity of natural convection sustained by isothermal concentration gradients. Following relation [\(11\)](#page-6-0), *Gri* is positive if the *i*–th species increases the local density of the medium and negative otherwise.

By writing the system viscosity as

$$
v = v_0 \times v_{rel}, \qquad (12)
$$

where v_0 represents the kinematic viscosity of the aqueous BZ mixture, we can conveniently use v_{rel} as a direct dimensionless parameter to control the system dynamics as in the experiments. This allows to vary at once both D_v and Gr_i .

The equations system [\(6–10\)](#page-5-1) is solved by using the Alternating Direction Implicit Method (ADI)^{[47](#page-8-19)} over the dimensionless spatial domain of length $L_x = 50$ and height $L_z = 50$, discretized with a 100×100 points grid. Solutions were not substantially altered by increasing the spatial grid density.

We apply no-slip boundary conditions for the fluid velocity (i.e. ψ = 0)^{[48](#page-8-20)} and no-flux boundary conditions for the chemical concentration fields at the rigid walls of the slab. Due to the stiffness of the Oregonator model, simulations are run using a small integration time step $h_t = 1 \times 10^{-5}$, that ensures numerically stable and convergent solutions.

Experimental data (namely spectrophotometric time series) report as a function of time the solution absorbance (which is directly correlated to the catalyst concentration) averaged over the spatial domain scanned by the spectrophotometric beam. To compare numerical simulations with real experiments, we build the simulation time series by reporting at each time step the mean concentration of the oxidized catalyst, $\langle c_2(x, z, t) \rangle$, averaged over the solving grid. The dynamics reported hereunder correspond to the transient regimes of the experiments where natural convection is fully set-in, i.e. after stirring is stopped and, if possible, transitions to aperiodic behaviour should be visible. These regimes are framed in the experimental time series shown above. Differently from experiments, the signals obtained in the simulations are stationary because, as mentioned above, the reactants depletion is neglected.

As a starting point of our parametric study, we consider the same value setting for which in our previous studies we obtained a chaos in the same system^{[22](#page-8-1)[,23](#page-8-2),27}: $Gr_1 = Gr_2 = 12.1, D_v = 58.5$. The route from chemical chaos to regular periodic oscillations is

Fig. 4 Chaotic oscillations (a) and related amplitude Fourier spectrum (b) obtained for the RDC equations [\(6–10\)](#page-5-1) with $v_{rel} = 1.00$.

Fig. 5 Time series (a) and related amplitude Fourier spectrum (b) of the quasi-periodic regime obtained for the RDC equations [\(6–10\)](#page-5-1) with v_{rel} = 1.10. $a = 9f_2 - 11f_2$, $b = 3f_2 - 2f_1$, $c = f_1 + f_2$, $d = 4f_2 + 2f_1$, $e = 3f_1 + f_2$.

then followed by increasing the relative viscosity of the medium, and, accordingly, reducing the starting value of *Gri* by a factor $1/v_{rel}^2$, and increasing D_v by v_{rel} . In agreement with the experimental results, the system undergoes different dynamical regimes corresponding to a RTN scenario:

Chaotic regime. In Figure [4a](#page-6-1) we show the typical aperiodic behaviour corresponding to $v_{rel} = 1.00$. Similar dynamics are found in the range $v_{rel} \in [1.00, 1.04]$. Within this parametric window the time series present high sensitivity to initial conditions and the signals diverge one from each other if the initial concentrations of the chemical species are slightly varied. This is consistent with one of the most striking signatures of chaos. Also in Fig. [1.](#page-4-0)b, there is the amplitude FFT spectrum of the signal in panel a). This shows a typical broadband, almost continuous, spectrum describing the infinite number of frequencies composing these chaotic oscillations, with a main contribution for small frequencies around 0.4. To further test and characterize for chaos, we calculated in a previous work^{[22](#page-8-1)} the largest Lyapunov exponent, λ , using the Rosestein algorithm from TISEAN package^{[49](#page-8-21)} and we obtained $\lambda = 0.018$. • Por marine de al contrar de la cont

Quasi-periodic regime. As the relative viscosity v_{rel} is increased to the value 1*.*05 a bifurcation to a quasi-periodic behavior is found (see Fig. [5\)](#page-6-2). The toroidal nature of the flow in the related phase space is confirmed by the Fourier amplitude spectrum in Fig. [5.](#page-6-2)b. Here we show the two fundamental frequencies $f_1 \sim 0.4$, $f_2 \sim 0.59$ characterising this regime, along with their main linear combinations and their harmonics. Note that the dominant contribution f_1 also present in the broadband spectrum of the chaotic regime is preserved. The ratio f_1/f_2 is an irrational number as expected for quasi-periodic oscillations.

Fig. 6 Time series (a) and related amplitude Fast Fourier spectrum (b) of the periodic regime obtained from the RDC equations [\(6–10\)](#page-5-1) with v_{rel} 1*.*24.

Periodic regime. In Fig. [6](#page-7-13) is shown a numerical experiment carried out for $v_{rel} = 1.24$. After a transient period (about 70 time units), the dynamics of the chemical species concentration switches to a regular periodic behaviour, here characterized by a limit cycle with one fundamental frequency $f_1 \sim 0.4$. Note that this frequency differs from that can be observed for the correthis frequency differs from that can sponding pure reaction-diffusion system $(f_1 \sim 0.75^{22})$, confirm-
ing the impact of the RDC interplay in the system dynamics. We ing the impact of the RDC interplay observed that the frequency of the periodic oscillations increases to this limit as v_{rel} is further increased beyond the threshold 1.23.

5 Conclusion

To summarize, we investigated the RDC coupling in a chemical oscillator as a general method to induce and control *in-situ* chaos. The transition from periodic to chaotic behaviours is chemically triggered by self-sustained oscillations that, coupled to diffusion, sustain pattern formation and, concretely, concentration heterogeneities. The related density gradients, if the action of the gravitational field is at play, start buoyancy-driven hydrodynamic flows that can feedback and complicate the spatio-temporal evolution of the reaction and even lead to cha

The RDC interplay can be suitably ruled both *via* kinetic and hydrodynamic parameters. Here we showed experimentally that by increasing the viscosity of the ferroin-catalyzed BZ medium through the introduction of micellar SDS ionic surfactant, we can prevent the onset of the fingerprinting chaotic transient normally observed in the BZ carried out in aqueous solution.

Numerical simulations of the corresponding RDC model, where the Oregonator model is coupled to fickian diffusion and Navier-Stokes equations, agree with experimental results. They reveal a transition from a chaotic to a periodic regime by following a Ruelle-Takens-Newhouse scenario when the relative viscosity, affecting both the dimensionless viscosity and the Grashof numbers, is increased. Because of the batch conditions, an improved model should take into account the consumption of the reagents during the reaction evolution, however we already faced and modelled this feature in a previous work²³. Though we use some strong approximations in the system modelling, experimental features are not only qualitatively reproduced, but we can also find a semiquantitative matching with simulations. In particular we observe that a comparable increment in the relative viscosity induces analogous effects in the system dynamics both in numerical and real And the same of t

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